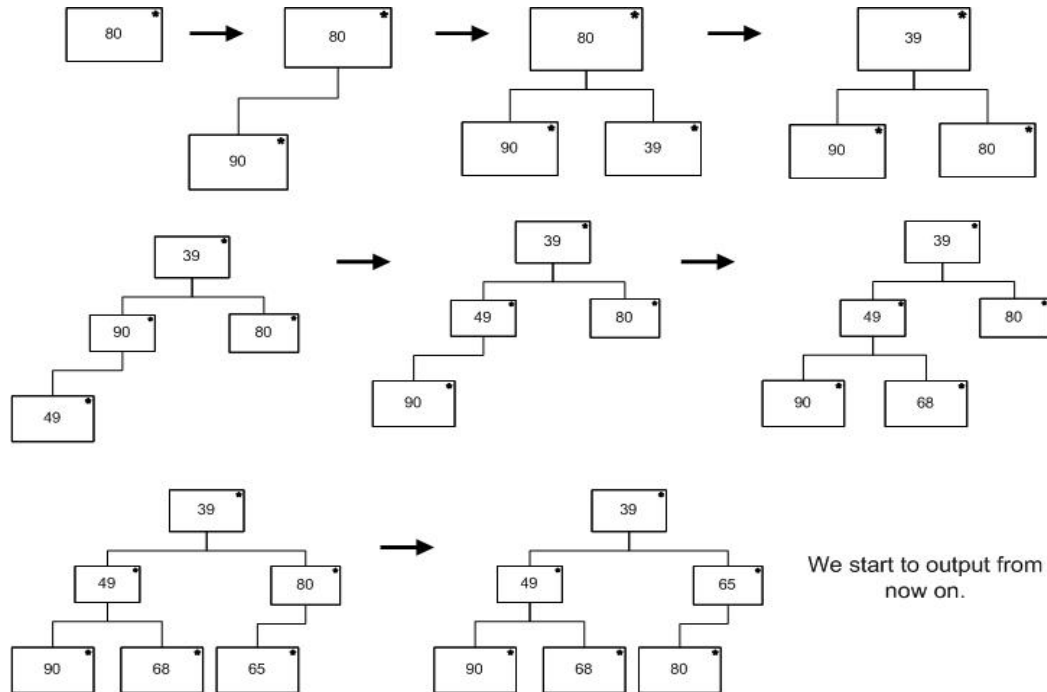
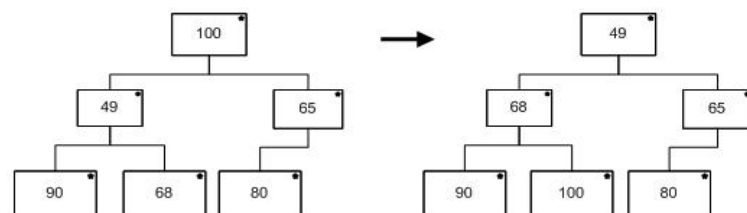


CS 351 – Homework 3

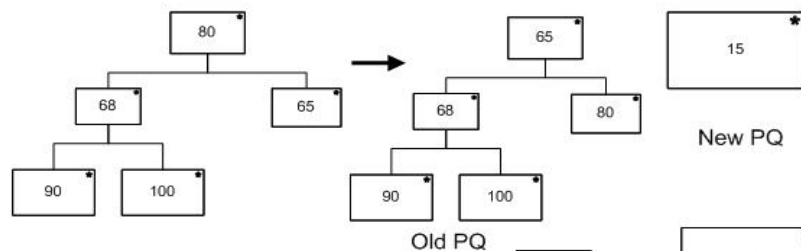
Answer 1.



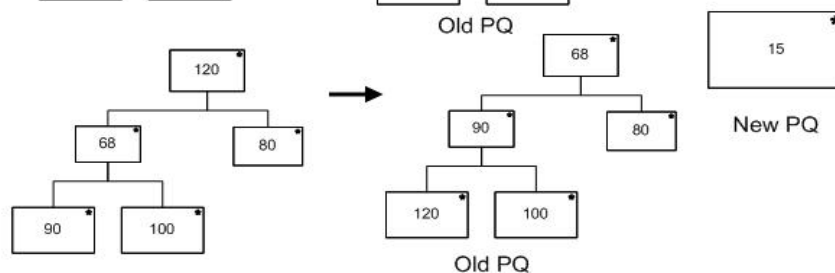
$100 > 39$, so the newcomer goes to the root of the current queue and we output the current root
Output Segment :39

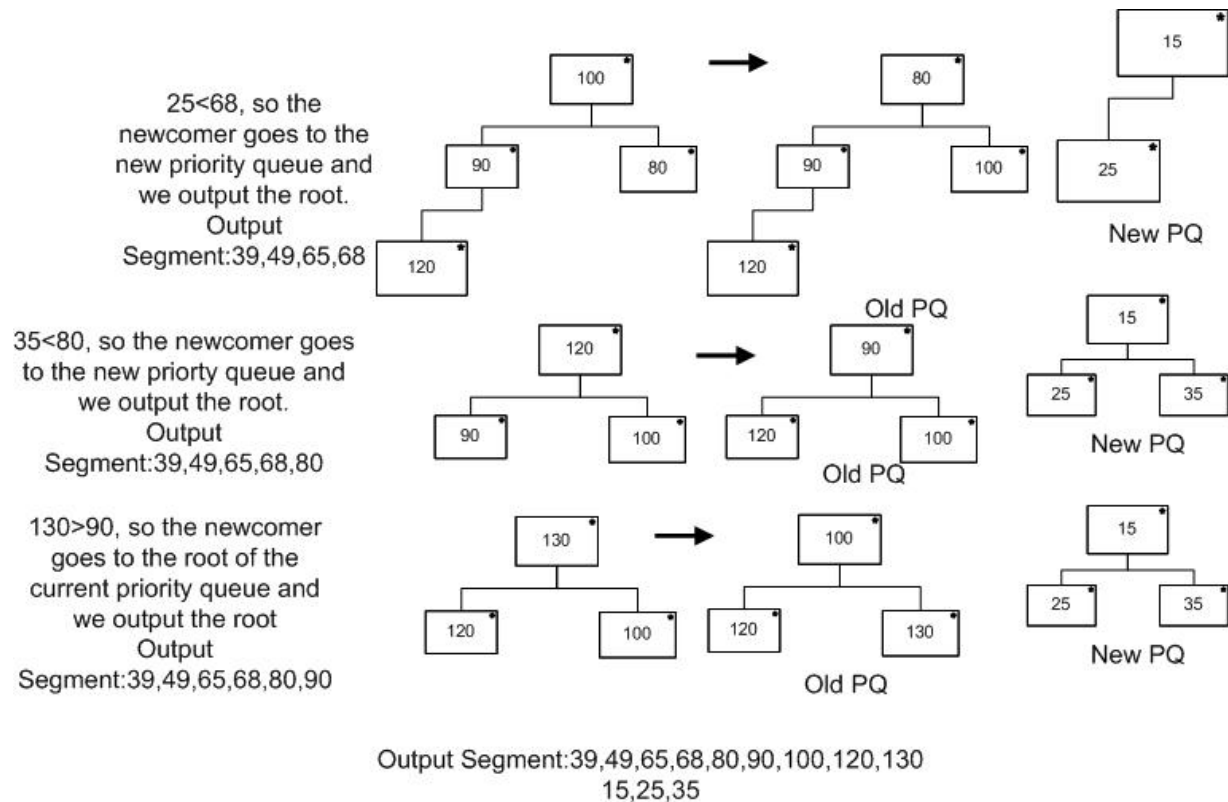


$15 < 49$, so the newcomer goes to the new priority queue and we output the current root.
Output Segment: 39,49



$120 > 65$, so the newcomer goes to the current priority queue and we output the root.
Output Segment:39,49,65





Answer 2.

HeapSort, unlike other sorting algorithms, can be executed overlapping the input and output. Only I/O time needs to be counted. So the answer is:

$$2 * b * ebt = 2 * 0.84 * [(400 * 10000000) / 2400]$$

$$2 * 0.84 * 1666666.7 = 2800000 \text{ms} = 2800 \text{seconds.}$$

Answer 3.

In the previous question we calculated the heap sort, now we need to calculate the merge times and add them together.

a) For 2-way merge time needed for one pass is $= 2 * p * nsg * (r+s) + 2 * b * ebt$
 $= 2 * 2 * 400 * (24.3) + 2 * 1666666.7 * 0.84 = 2838880 \text{ ms}$
 We have $\text{ceiling}[\log_2(400)] = 9$, we have 9 passes, so

$9 * 2838880 = 25549920 \text{ms}$ and we need to add time on answer 2.
 Total time is $= 7.09 \text{ hours} + 0.78 \text{hours} = 7.87 \text{ hours}$

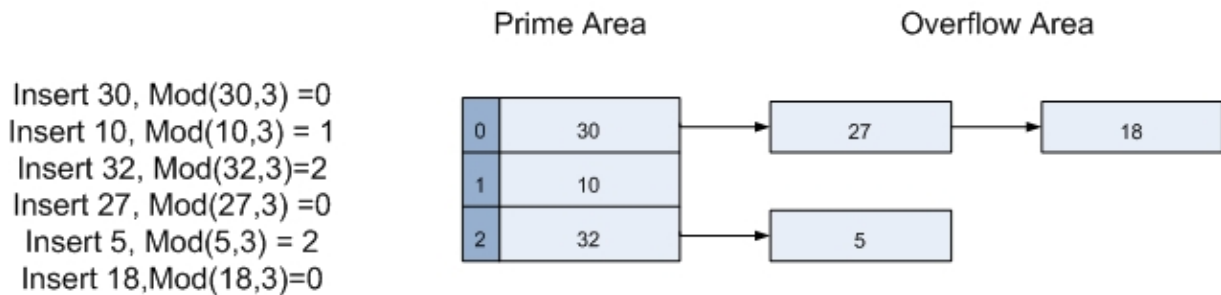
b) For 4-way merge time needed for one pass is $= 2 * 4 * 400 * (24.3) + 2 * 1666666.7 * 0.84$
 $= 2877760 \text{ms}$
 We have $\text{ceiling}[\log_4 40] = 5$, we have 5 passes, so $5 * 2877760 = 3.99 \text{ hours}$

We need to add the time on answer two, so the total time is $3.99 + 0.78 = 4.77$ hours

c) For this question P is 400, we can use a specialized formula since only one pass is needed.

$$4 * ebt * b + 2 * (nsg)^2 * (r+s) = 4 * 0.84 * 1666666.7 + 2 * (400)^2 * 24.3 = 3.71 \text{ hours}$$

Answer 4.



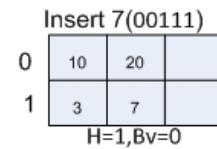
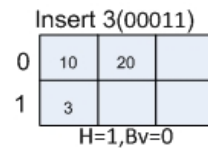
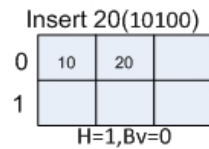
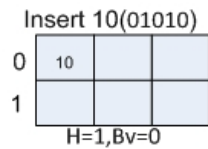
- To find 18, 3 disk accesses is required because first access will be to prime area, second access for first entry in the overflow area and on the third access 18 is retrieved.
- For 30, 10 and 32 one disk access is required, for 27 and 5, two disk access is required and for 18, three disk accesses is required and we have 6 entries. The average number of accesses for successful search is $= \frac{1+1+1+2+2+3}{6} = 1.666$
- For entries which have $\text{Mod}(\text{entry},3) = 0$, three disk accesses is required for unsuccessful search, for entries which have $\text{Mod}(\text{entry},3)=1$, 1 disk access is required and for entries which have $\text{Mod}(\text{entry},3)=2$, 2 disk accesses is required. So $(3 + 1 + 2)/3 = 2$

Answer 5.

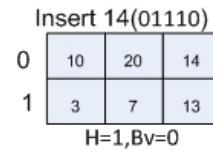
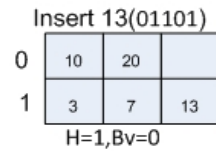
Pseudo Key	Key	Pseudo Key In Binary
10	10	01010
20	20	10100
3	3	00011
7	7	00111
13	13	01101
14	14	01110
17	17	10001
21	21	10101
25	25	11001
16	16	10000
22	22	10110
30	30	11110

We start from $h=1$, $B_v=0$, Insertions illustrated below.

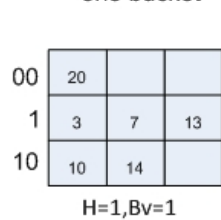
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Sec03



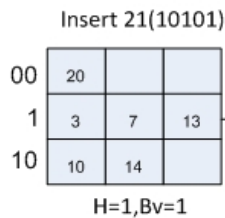
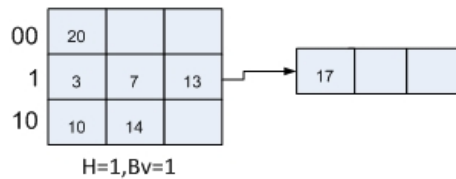
At this point, we reach the desired load factor(2/3). From now on, we will add $2/3 \cdot 3 = 2$ entries and add one bucket



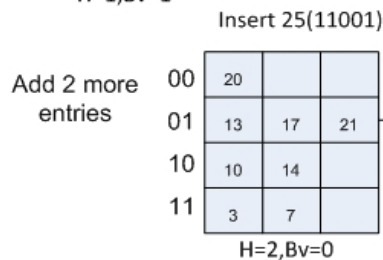
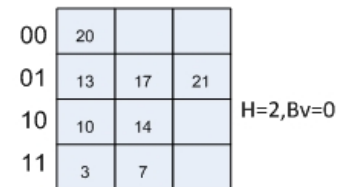
Now we add one bucket.



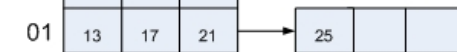
Add 2 more entries



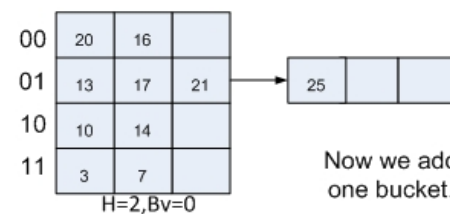
Now we add one bucket.



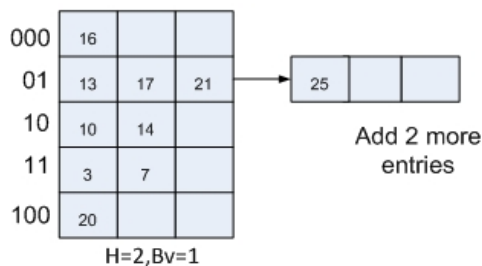
Add 2 more entries



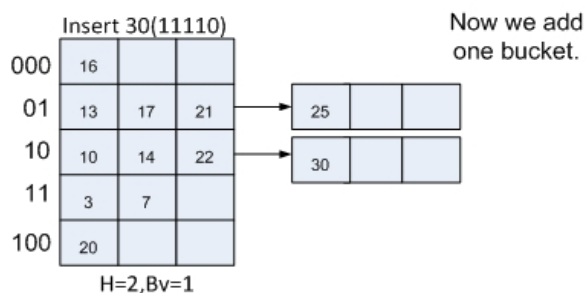
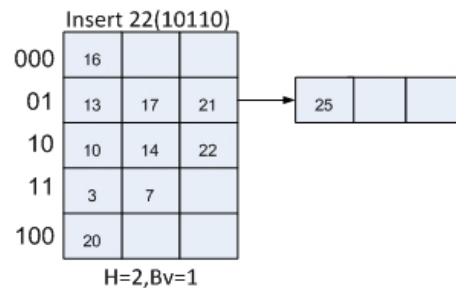
Insert 16(10000)



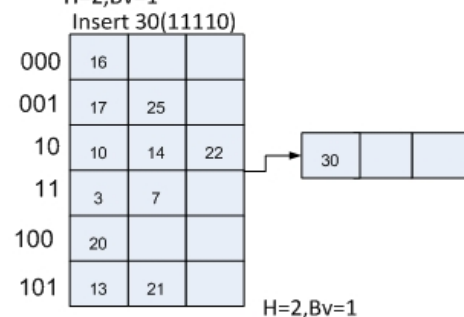
Now we add one bucket.



Add 2 more entries



Now we add one bucket.



Answer 6.

For $bv=5$, $h=5$;

In linear hashing, blocks hashed at level $h+1$ are: $[0, bv-1]$ and $[2^h, n-1]$ n being the number of blocks. There are 5 blocks in $[0, bv-1]$ interval. The other part always has the same quantity. So the blocks hashed at level $h+1$ is 10.

Blocks hashed at level h are in the interval $[bv, 2^h-1]$ which is 27.

The binary address of the last bucket of the file is 100100.

The binary address of the last bucket hashed at level 5 is 11111.

For $bv=0$, $h=5$;

In linear hashing, blocks hashed at level $h+1$ are: $[0, bv-1]$ and $[2^h, n-1]$ n being the number of blocks. There are 0 blocks in $[0, bv-1]$ interval. The other part always has the same quantity. So the blocks hashed at level $h+1$ is 0.

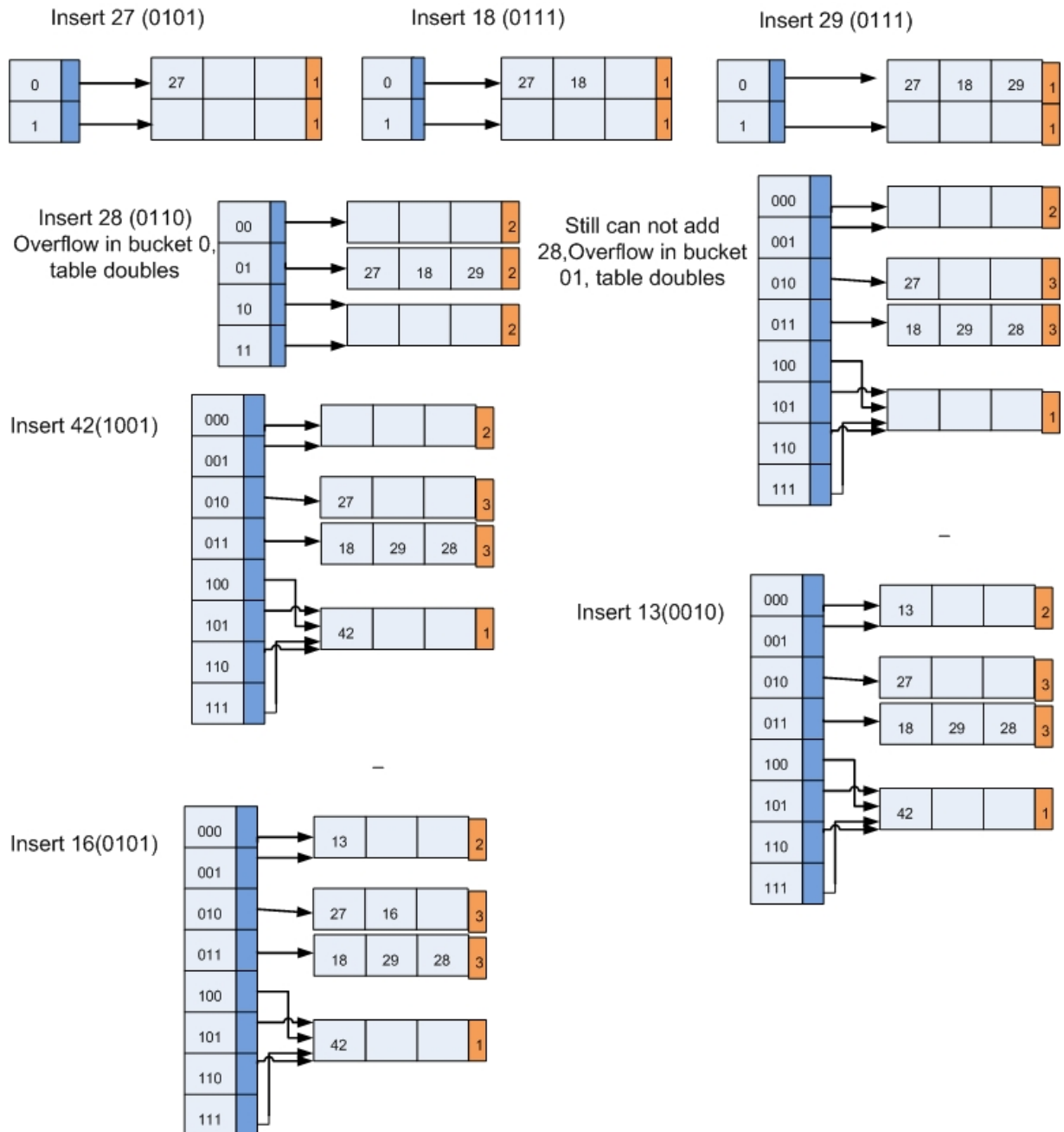
Blocks hashed at level h are in the interval $[bv, 2^h-1]$ which is 32.

The binary address of the last bucket of the file is obviously 11111.

The binary address of the last bucket hashed at level 5 is 11111.

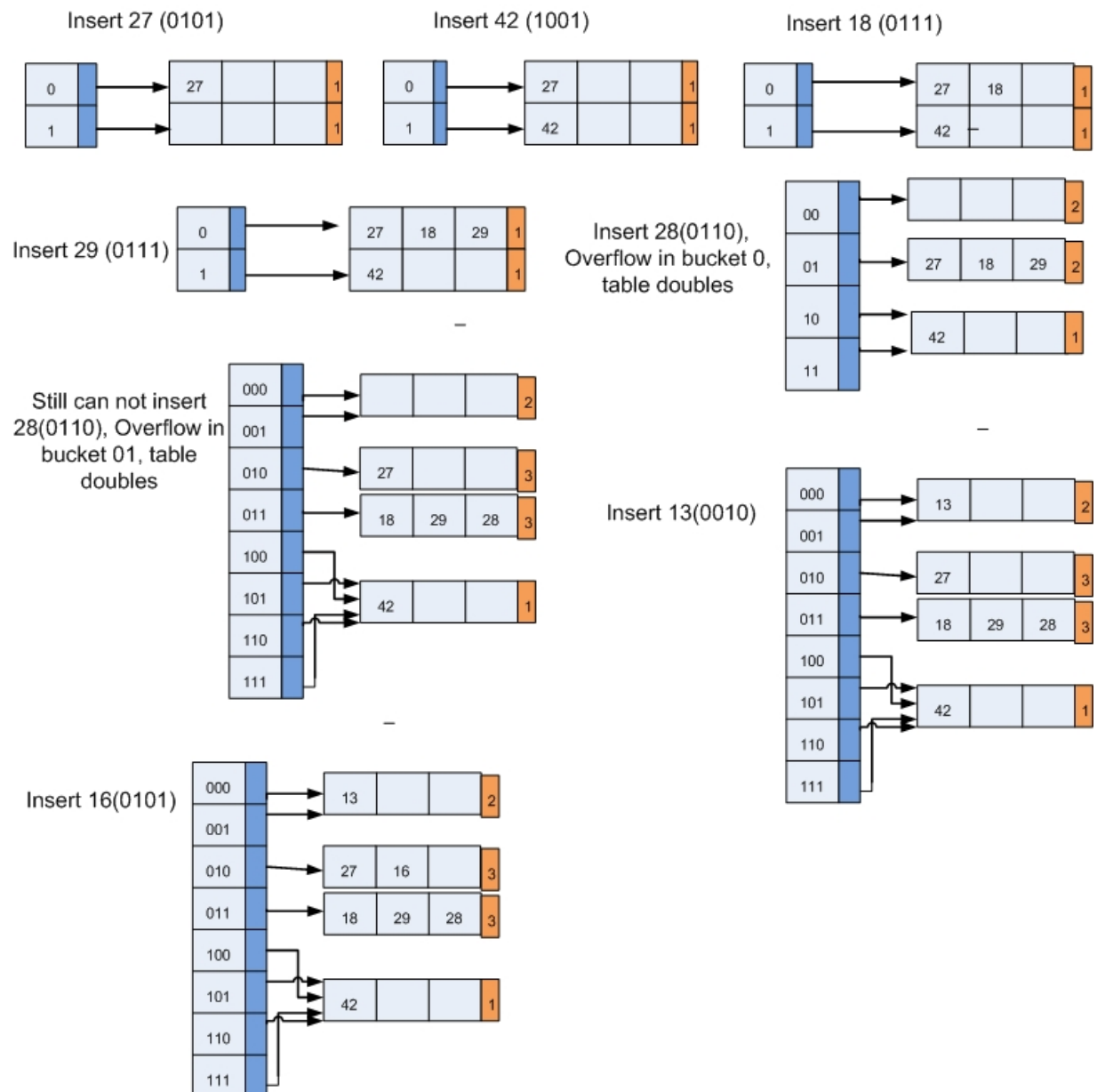
Answer 7.

Key Value	Pseudo Key	Binary Pseudo Key
27	5	0101
18	7	0111
29	7	0111
28	6	0110
42	9	1001
13	2	0010
16	5	0101



Answer 8.

Key Value	Pseudo Key	Binary Pseudo Key
27	5	0101
42	9	1001
18	7	0111
29	7	0111
28	6	0110
13	2	0010
16	5	0101



Safa Erişti
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Directory size does not change, it is 8 for questions 7 and 8. Number of data pages, which is 4, is the same also, because no matter how we put the numbers, entries will go to the same place and table will increase accordingly.